



A four-wing attractor

This application note describes a rather beautiful “four-wing attractor”, which is due to [WANG et al. 2009]. In this paper the authors analyse a general chaotic system of three coupled differential equations of the form

$$\dot{x} = ax + cyz$$

$$\dot{y} = bx + dy - xz$$

$$\dot{z} = ez + fxy.$$

A particularly beautiful attractor results from the parameter set $a = 0.2$, $b = -0.01$, $c = 1$, $d = -0.4$, $e = -1$, and $f = -1$. The resulting set of equations

$$\dot{x} = 0.2x + yz$$

$$\dot{y} = -0.01x - 0.4y - xz$$

$$\dot{z} = -z - xy$$

is easy to scale since a quick numeric experiment shows that x , y , and z are well within the interval $[-3, 3]$, so that scaling coefficients $\lambda_x = \lambda_y = \lambda_z = \frac{1}{3}$ may be used. The resulting scaled system of equations is then

$$\dot{x} = 0.2x + 3yz$$

$$\dot{y} = -0.01x - 0.4y - 3xz$$

$$\dot{z} = -z - 3xy,$$

which can be implemented directly on an analog computer.¹

The resulting analog computer setup is shown in figure 1. Figures 2 and 3 show the behavior of this system in the y/z - and x/y -plane respectively.²

Happy analog computing! :-)

¹Since it requires three products either two coupled THE ANALOG THINGS or an external multiplier such as the AD633 are required.

²It may be necessary to twiddle the parameter 0.01 slightly to get a nice result.

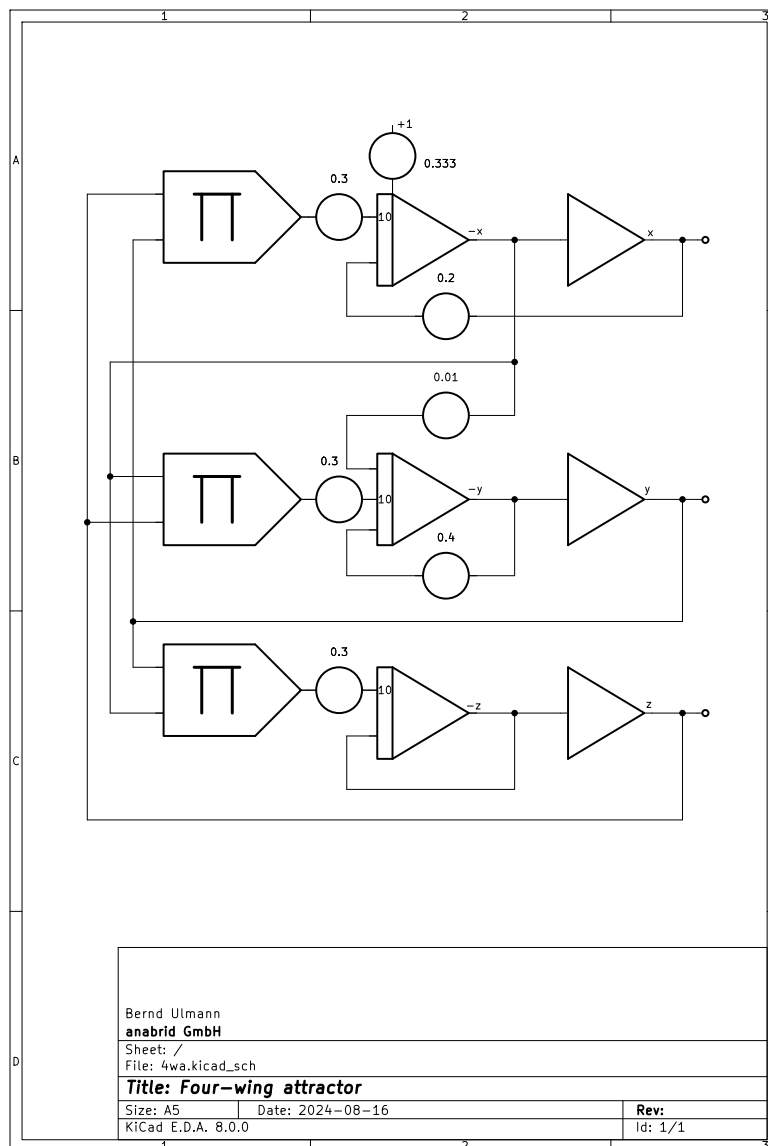


Figure 1: Analog computer setup for the three time scale system

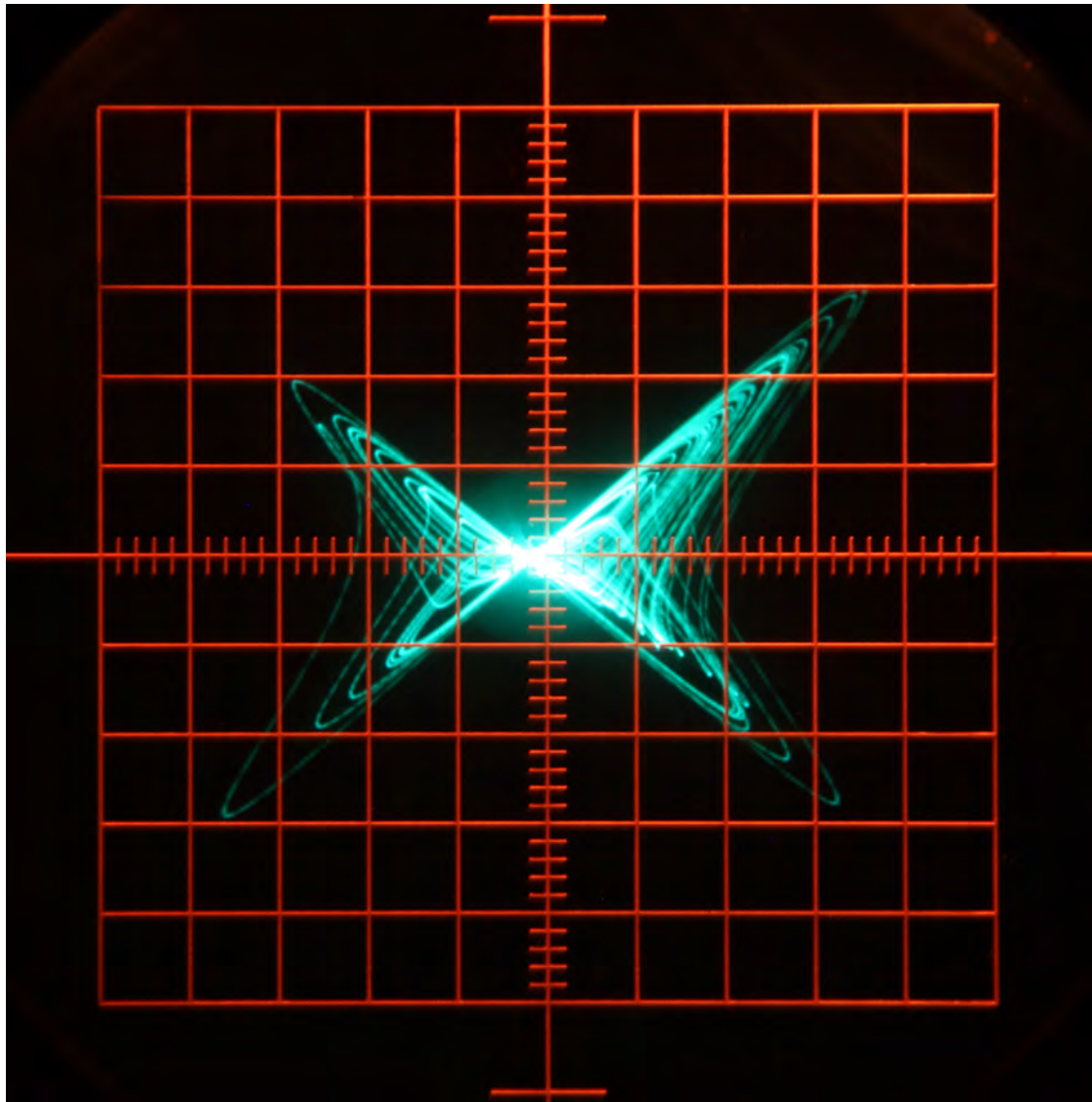


Figure 2: Four-wing attractor in the y/z -plane

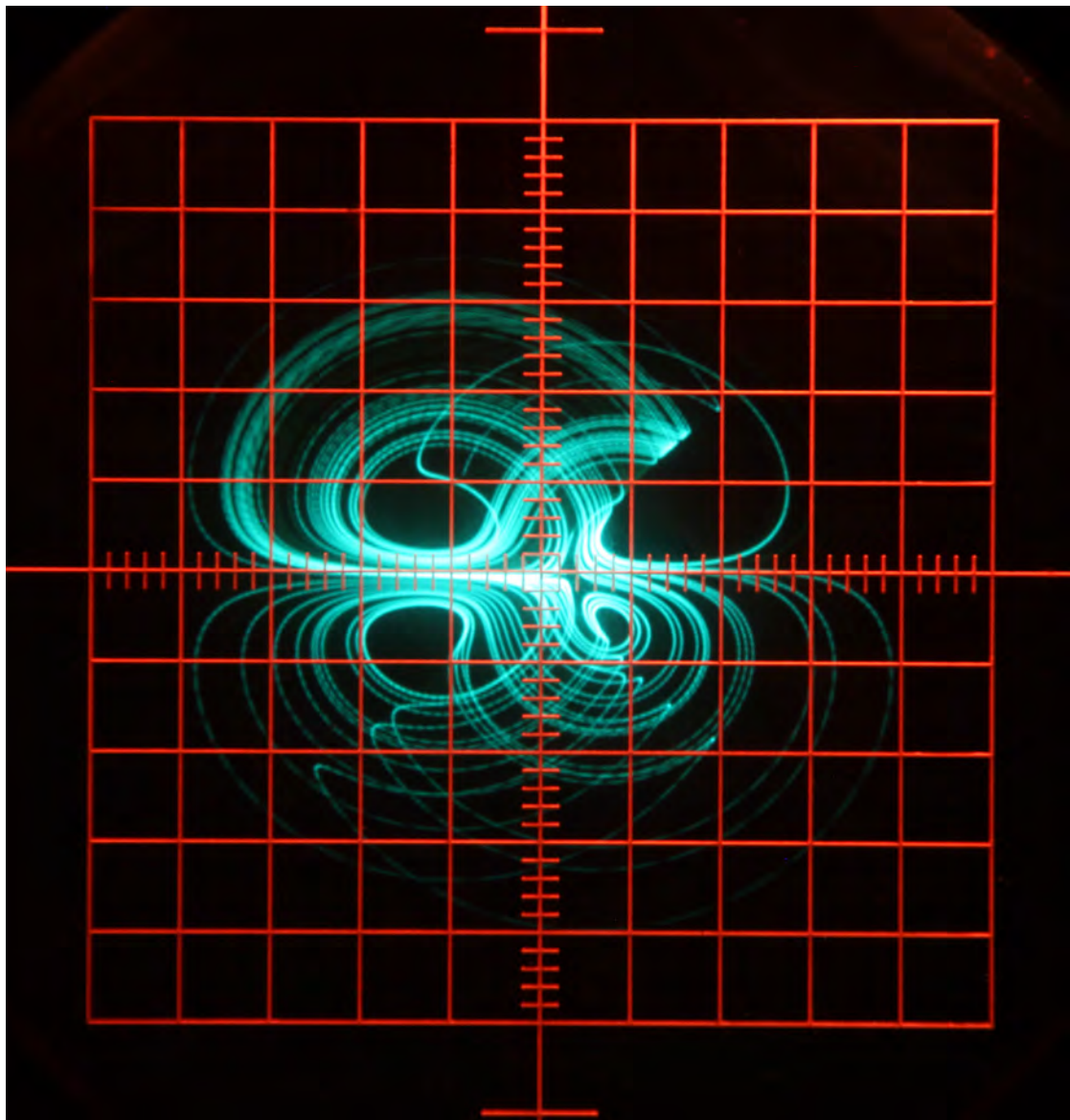


Figure 3: Four-wing attractor in the x/y -plane



Analog Computer Applications

References

- [WANG et al. 2009] ZENGHUI WANG, YANXIA SUN, JACOBUS VAN WYK, GUOYUAN QI, MICHAEL ANTONIE VAN WYK, "A 3-D four-wing attractor and its analysis", in *Brazilian Journal of Physics*, vol. 39, no. 3, September, pp. 547–553