

## Yet another LORENZ system

Recently, I stumbled over PETER MCNAIR's great blog *Analog Ontology*,<sup>1</sup> where he describes – among many other highly interesting things – his implementation of a rather unknown attractor devised by EDWARD N. LORENZ. In 1984 LORENZ published a paper titled *Irregularity: a fundamental property of the atmosphere*<sup>2</sup> where he describes a system of three coupled differential equations:

$$\begin{aligned}\dot{x} &= -y^2 - z^2 - ax + af \\ \dot{y} &= xy - bxz - y + g \\ \dot{z} &= bxy + xz - z\end{aligned}$$

The parameters of this system are  $a = \frac{1}{4}$ ,  $b = 4$ ,  $f = 8$ ,  $g = 1$ .

Scaling this system is pretty straight-forward as a quick numerical experiment shows:  $|x|$  and  $|y|$ ,  $|z|$  are bounded by 2 and 3, respectively. The resulting analog computer program is shown in figure 1. Tweaking the parameters is quite interesting, a typical set of solutions is shown in figure 2.

### References

[LORENZ 1984] EDWARD N. LORENZ, *Irregularity: a fundamental property of the atmosphere*, *Tellus* (1984), 36A, pp. 98–110

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<sup>1</sup><http://analog-ontology.blogspot.com/>

<sup>2</sup>See [LORENZ 1984].

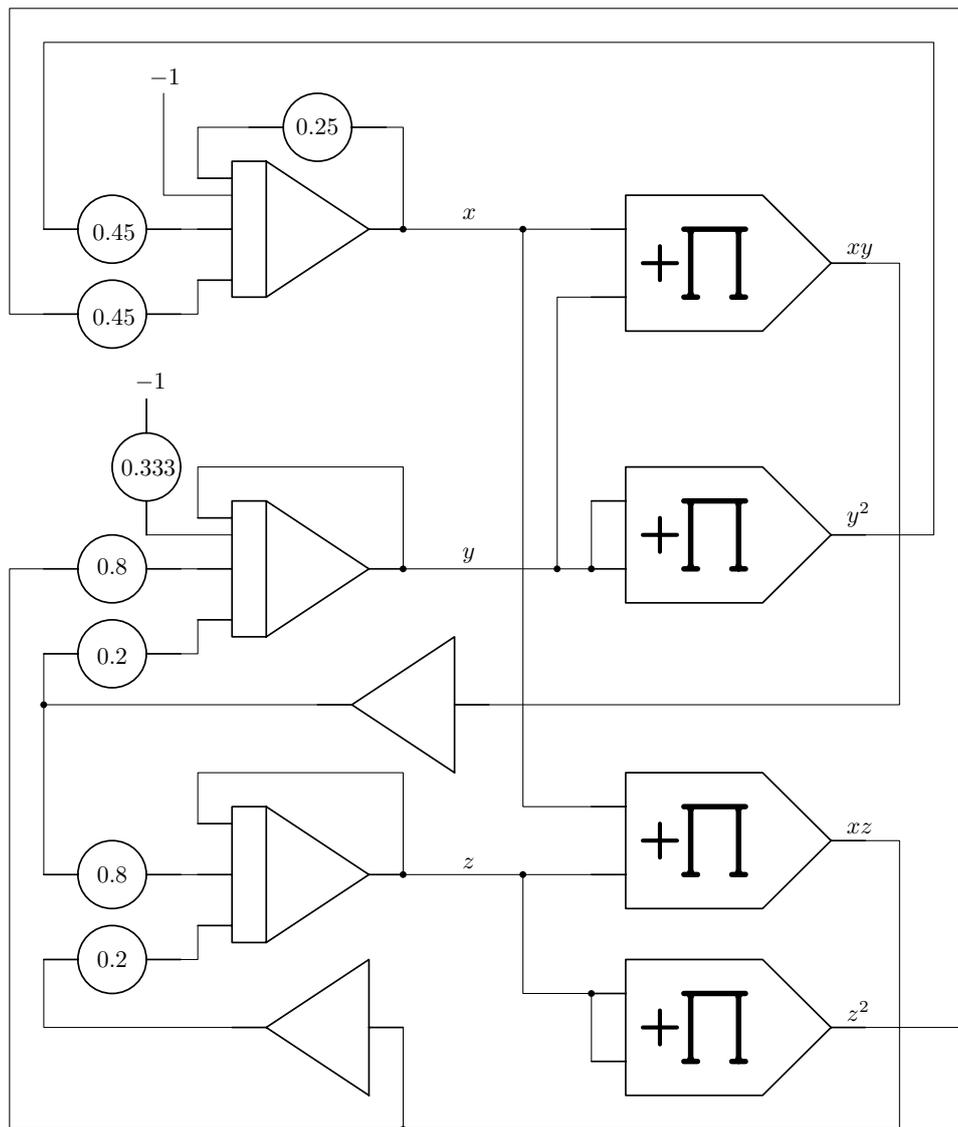


Figure 1: Program for the chaotic LORENZ-84 system

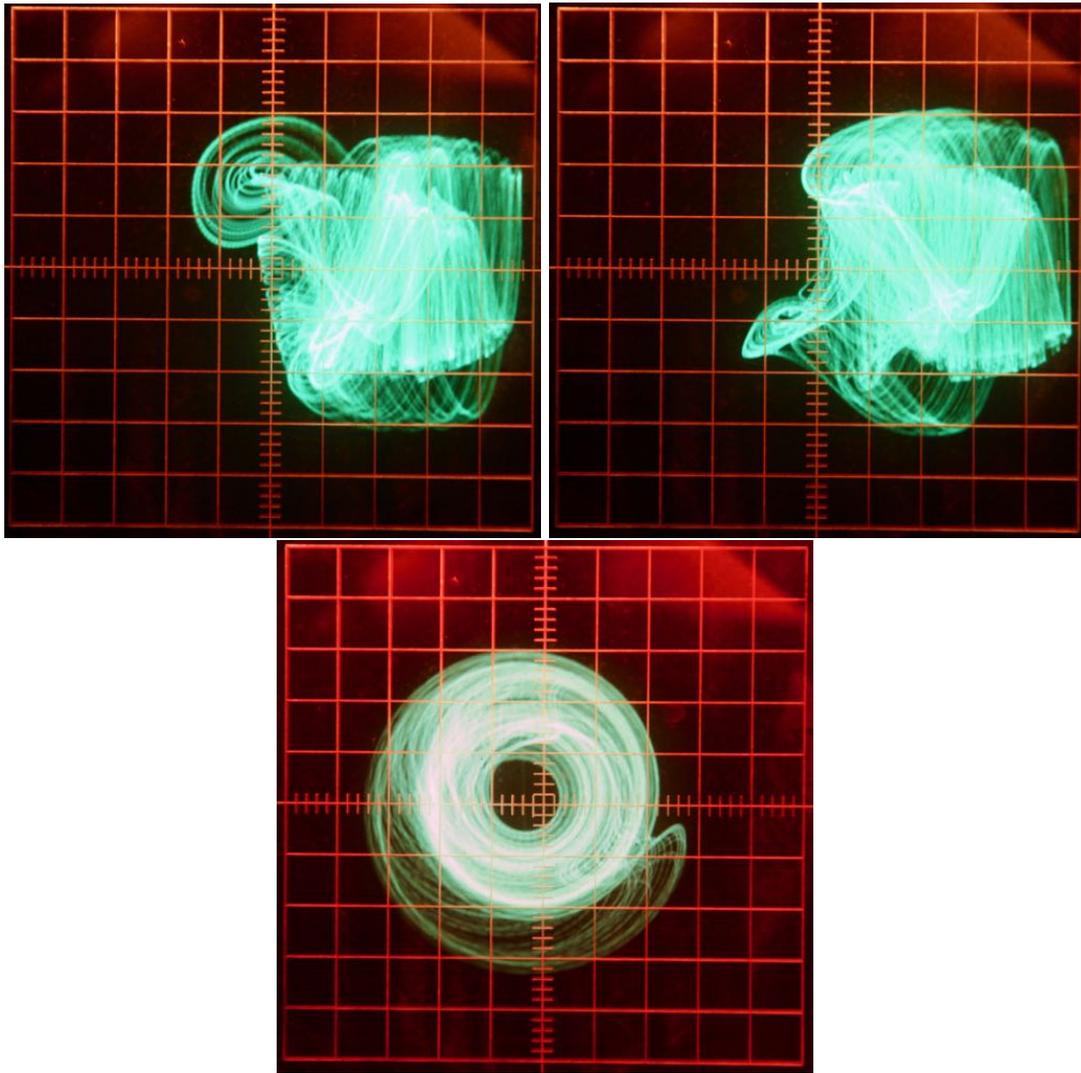


Figure 2: Typical behavior of the LORENZ-84 system, the three screen shots show  $x$  vs.  $y$ ,  $x$  vs.  $z$ , and  $y$  vs.  $z$